

The Theoretical Minimum

Classical Mechanics - Solutions

L03E02

Last version: tales.mbivert.com/on-the-theoretical-minimum-solutions/ or github.com/mbivert/ttm

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Exercise 1. *Integrate this equation. Hint: Use definite integrals.*

The equation in question resulting from Newton's second law in the case of a constant force F_z being applied to an object of mass m following the z -axis:

$$\dot{v}_z = v_z'(t) = \frac{F_z}{m}$$

By integrating both sides, thanks to the fundamental theorem of calculus, assuming the mass is constant over time, we obtain:

$$\begin{aligned}v_z(t) &= \int \frac{F_z}{m} dt \\ &= \frac{F_z}{m} \int dt \\ &= \frac{F_z}{m} t + c, c \in \mathbb{R}\end{aligned}$$

Generally, c would be determined from an initial condition $v_z(0)$, which in our case, would precisely be c , hence:

$$\boxed{v_z(t) = v_z(0) + \frac{F_z}{m} t} \quad \square$$

Which is exactly the solution proposed in the book.